# Errata file for "Intermediate Microeconomic Theory: Tools and Step-by-step Examples," MIT Press

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October 18, 2023

# 1. Chapter 2.

- Page 13, Example 2.2, second paragraph should read "In addition, he says that there are other bundles different from A and D making him happier than D does.
- Page 18, Example 2.5, last sentence should read "As in the case of  $MU_x$ , we find there that...".
- Page 19, Example 2.6:
  - First sentence after the displayed equation should read "which is negative for any positive amounts of goods x and y."
  - Last sentence should read "for all positive values of x and y."
- Page 22.
  - Line 4 should read "...than the horizontal intercept 9/5 = 1.8 "
  - Line 7 should read "...where we have  $y \simeq 1.33$ ."
- Page 23.
  - Second paragraph should refer to figure 2.5 rather than 2.3b.
  - Footnote 6, line 2, should read "...an indifference curve  $y = \frac{10+ax}{b} = \frac{10}{b} + \frac{a}{b}x$ , which increases in..."
- Page 37, third line should read "...she is poorer than individual 2. In contrast, when individual..."
- Page 39, Exercise 7(a) should read "For a given utility level of 10, find the..."
- Page 41, Exercise 15, lines 3-4 should read "Relative to envy preferences in exercise 14, guilt preferences reduce Peter's utility..."

# 2. Chapter 3.

- Page 46, last paragraph should read "At the horizontal (vertical) intercept, the consumer spends..."
- Page 50, previous to last sentence should read  $u(x, y) = ax^2 by$ , where a, b > 0 and..."
- Page 51, first sentence, immediately before Tool 3.1, should add "For simplicity, this chapter only considers utility function that produce strictly convex indifference curves (such as the Cobb-Douglas and perfect complements) or linear indifference curves (such as perfect substitutes)."
- Page 52,
  - Step 2a, after the displayed equation should read "...which yields  $\frac{100}{30} \simeq 3.33$  units."
  - Step 4: at the end should read "...tangency condition  $y = x \simeq 3.33$  units."

- Page 58. Example 3.4. The last ratio, at the end of the first paragraph, should read  $\frac{I'}{p'_x}$  instead of  $\frac{I'}{p_x}$ .
- Page 62. Example 3.5.
  - The second displayed equation should read

$$y = \left(\frac{100}{5} - \frac{4-1}{5}2\right) - \frac{1}{5}x = \left(20 - \frac{3}{5}2\right) - \frac{1}{5}x = \frac{94}{5} - \frac{1}{5}x$$
 for all  $x > 2$ .

- The previous-to-last line in example 3.5 should read -0.2, thus becoming flatter..."

• Page 64: At the middle of the page, equation  $\frac{\partial \mathcal{L}}{\partial u}$  should read

$$\frac{\partial \mathcal{L}}{\partial y} = MU_y - \lambda p_y = 0$$
, and

- Page 67.
  - Step 2a, second line should read "from step 1, y = x, in the constraint..."
  - Example 3.8, second line should read "utility from example 3.3,..."
- Page 68, Step 2a, fourth line should read "...we obtain  $y \simeq 1.08$  units."

#### 3. Chapter 4.

- Page 81, figure 4.2b (right panel) should be have an inverted-U shape: first increasing with income, then decreasing with income.
- Page 94. Self-assessment 4.9, close to the end of the page, should read "... utility function is  $u(x, y) = 3x^{1/2} + 4y$ , her income is...".
- Page 96, last paragraph, second line should read "...to the decomposition bundle B,  $L_B L_A$ , whereas the income effect..."
- Page 101, line 4 should read "... $\simeq -5.55$  units."
- Page 102, exercise 3(b) should read "Find the new demand function for each good."
- Page 103, exercise 8, last sentence should read "...and income effects from this price change."

#### 4. Chapter 6.

- Page 132, Example 6.3: Please remove the \$ sign inside the square roots.
- Page 134, footnote 4, line 2, should read "... positive for all income levels I > 0."
- Page 136, footnote 6, line 2: should read "which is positive for all I > 0, implying that..."
- Page 136, footnote 6, line 3, should read "which is also positive for all I > 0, thus indicating..."
- Page 145.
  - Line 3, please remove the \$ sign inside the square roots.
  - Example 6.11. The sentence after the first displayed equation of the example should read "which simplifies to  $\sqrt{\$3,000} > \frac{6}{7}\sqrt{\$4,000}$ , or 54.77 > 54.21. In addition, lottery *D* is preferred to *C* in Choice 2. Assuming that g(x) = 2, as in previous examples, but g(y) now increases to g(y) = 9, we find that lottery *D* is preferred to *C* if and only if

$$\begin{array}{l} \displaystyle \frac{9 \times 0.2}{(9 \times 0.2) + (2 \times 0.8)} \sqrt{\$4,000} + \frac{2 \times 0.8}{(9 \times 0.2) + (2 \times 0.8)} \sqrt{\$0} \\ \\ \displaystyle > \quad \frac{9 \times 0.25}{(9 \times 0.25) + (2 \times 0.75)} \sqrt{\$3,000} + \frac{2 \times 0.75}{(9 \times 0.25) + (2 \times 0.75)} \sqrt{\$0} \end{array}$$

which simplifies to  $\frac{9}{17}\sqrt{\$4,000} > \frac{3}{5}\sqrt{\$3,000}$ , or 33.48 > 32.86. Therefore, the experimental observations..."

• Bottom of page 147. The displayed equation should have exponent 1/2. This also applies to the in-line equation in the subsequent paragraph (second line), which should also have exponent 1/2.

#### 5. Chapter 7.

- Page 156, Example 7.1, end of second paragraph should read "...level of 1 0.77 = 0.23."
- Page 170, third line, should read "...vertical line because ratio  $\frac{q}{Aa}$  is not a function..."
- Page 171, immediately before the first displayed equation, should read "In addition, the slope of the isoquant..."

# 6. Chapter 8.

- Page 187. Immediately before Tool 8.1, should read "This tool applies to production functions that generate strictly convex and linear isoquants."
- In page 190, "this input demand", in the middle of the page, should read "these input demands".
- In page 191, at the bottom of the page (immediately before Self-assessment 8.5), the in-line equation should have ratio  $\frac{q}{8}$  rather than  $\frac{q}{2}$ .
- In Example 8.7 (page 194), the in-line equation 4r < w should read r < 4w everywhere it shows up. Similarly, the inequality 4r > w should read r > 4w everywhere. These two changes apply to Example 8.7 and all subsequent examples in this chapter.
- In Example 8.10 (page 201), the displayed equation at the top of the page should read

$$\varepsilon_{TC,q} = \frac{\partial TC}{\partial q} \frac{q}{TC} = \frac{r}{8} \frac{q}{r\frac{q}{8}} = 1$$

The paragraph following this equation should read "which means that, if the firm seeks to produce 1 percent more units of output, its total costs increase by exactly one percent. (A similar argument applies if input prices satisfy 4r > w, where  $TC = w\frac{q}{2}$ , where output elasticity also becomes  $\varepsilon_{TC,q} = 1$ , which we leave for the reader as an exercise.)"

## 7. Chapter 9.

- Page 224. Example 9.5. Second line in the last paragraph should read "...price of p =\$1.32 at N = 61.62 firms."
- Page 229. Second displayed equation has a missing sign, so it should read  $-5 + 4q = \frac{5}{q} 5 + 2q$ . The remaining calculations in Example 9.4 are correct.
- Page 239, last displayed equation. Its last term should read  $2 \times 2$  (as in two times two) in the denominator, rather than  $2p_1$ .

## 8. Chapter 10.

- Page 248.
  - Seventh line should read "implying that the total cost of a single firm producing q units is lower than that of two firms that together produce q units, that is,  $TC(q) < TC(q_1) + TC(q_2)$ , where  $q = q_1 + q_2$ .
  - Footnote 1 should read "For instance, if TC = 100 + 2q, the cost of producing q = 10 units by a single firm is TC(10) = \$120, whereas the aggregate cost of two firms producing 5 units each is TC(5) + TC(5) = 110 + 110 = \$220. A similar argument applies to firms with total cost function of the form TC(q) = a + bq, where a, b > 0, since the aggregate cost of two firms producing  $\frac{q}{2}$  units each is  $TC\left(\frac{q}{2}\right) + TC\left(\frac{q}{2}\right) = \left(a + b\frac{q}{2}\right) + \left(a + b\frac{q}{2}\right)$ , which simplifies to 2a + bq, which is larger than the total cost of a single firm producing q units, TC(q) = a + bq."
- Page 261. The second displayed equation should have  $(q_1 + q_2)$  multiplied times the second term, so it should read  $p(q_1, q_2) + \frac{\partial p(q_1, q_2)}{\partial q_1}(q_1 + q_2) = \frac{\partial TC_1(q_1)}{\partial q_1}$ . A similar comment applies to the third displayed equation, which should read  $p(q_1, q_2) + \frac{\partial p(q_1, q_2)}{\partial q_2}(q_1 + q_2) = \frac{\partial TC_2(q_2)}{\partial q_2}$ .

• Page 262. Last line should read "...of  $\frac{q_1}{Q} = \frac{5}{14} \simeq 0.35$  in the US plant, and the remaining  $\frac{q_2}{Q} = \frac{9}{14} \simeq 0.64$  in the Chilean..."

# 9. Chapter 11.

• Figure 11.2, in the middle of the horizontal axis, the label should read  $q^{FD} = q^{PC}$ .

#### 10. Chapter 12.

- Page 297, first line should add a space so it reads "...in economics, a discussion..."
- Page 298 should read "we consider an scenario"
- Page 299, second paragraph, second sentence, should read "...this requires that every player maximizes his utility and that he knows the rules of the game..."
- Page 300, last paragraph should read "When strategy  $s_i$  strictly dominates every other strategy  $s'_i$ , we say that..."
- Page 301. Tool 12.1, fix the step numbering.
- Page 307. Tool 12.2, fix the step numbering.
- Page 316, last paragraph, should read "have a NE" rather than "have an NE" in both instances.
- Page 320, immediately after the last displayed equation should read "...when the goalie dives left..."
- Page 320, last paragraph should read "Do all games have a msNE with at least one player randomizing her strategies? Not necessarily..."
- Page 321, last line of the first paragraph should read "... or a msNE)."

#### 11. Chapter 13.

• Page 336, last paragraph should read "...the smallest subgame that we can circle is the one initiated after...". The end of this paragraph should read "Circles that break firm 2's..."

#### 12. Chapter 14.

- Page 357.
  - In the first displayed equation, percentages are omitted. The equation should read

$$HHI = \left(\frac{100}{1,000}\right)^2 + \left(\frac{100}{1,000}\right)^2 + \ldots + \left(\frac{100}{1,000}\right)^2$$
$$= 1,000 \left(\frac{100}{1,000}\right)^2 = 10.$$

– Similarly, in the same page, for an industry with  $N \geq 1$  firms, the second displayed equation should read

$$HHI = \left(\frac{100}{N}\right)^2 + \left(\frac{100}{N}\right)^2 + \dots + \left(\frac{100}{N}\right)^2$$
$$= N\left(\frac{100}{N}\right)^2 = \frac{10,000}{N},$$

- Page 361, first displayed equation, second line. Number 2 in the numerator should be deleted.
- Page 362.

- First displayed equation should read

$$p^* = p\left(\frac{a-c}{3b}, \frac{a-c}{3b}\right) = a - b\left(\frac{a-c}{3b} + \frac{a-c}{3b}\right)$$
$$= a - \frac{2(a-c)}{3b}$$
$$= \frac{a+2c}{3}.$$

- Last sentence immediately before example 14.1 should read "This can be alternatively expressed as  $\pi_i^* = b(q^*)^2$ ."
- Page 366.
  - First line should read "...two firms produce a homogeneous good..."
  - Paragraph 1(a), fifth line should read "...where  $\varepsilon \to 0$  indicates a small reduction..."
  - Footnote 7 should add the following sentence at the end "Generally, the small price reduction,  $\varepsilon$ , requires that  $\varepsilon < p_2 c$  to ensure that firms do not make a loss. Then, extremely small price reductions,  $\varepsilon \to 0$ , satisfy this requirement."
- Page 367.
  - Second line, the in-line equation should read " $p'_2 = p_1 \varepsilon$ , where  $\varepsilon \to 0$  is a small number..."
  - Last paragraph should read "...by a small amount,  $\varepsilon$ , so that  $p_i = p \varepsilon$ , where  $\varepsilon \to 0$ ."
- Page 368.
  - Figure 14.6, its top label should read  $p \varepsilon$ , rather than  $p_i \varepsilon$ .
  - Example 14.3, sixth line, should read " $Q^* = 12 c$ ", rather than Q = 12 c.
- Page 370.
  - Last displayed equation should not have star symbol, so it starts with " $\pi_i =$ ".
  - The last sentence of example 14.4 should read "...were only  $\pi_i^* = \frac{64}{9} \simeq$ \$7.11."
- Page 373. Self-assessment 14.6, second line should read "...during each of the two periods before the..."
- Page 374. Second displayed equation should read  $a bq_1 2q_2 c = 0$ .
- Page 376.
  - Example 14.7 should be numbered Example 14.6.
  - The last paragraph of this example should read "...for the leader,  $q_1^* = 4$  units, which entails  $q_2^* = \frac{4}{2} = 2$  units for the follower. In this scenario,..."
- Page 378, last line should read "...in equilibrium output,  $q_i^* = q_j^* = q^*$ , which yields..."
- Page 379. Example 14.8 should be numbered Example 14.7.
- Page 380, last paragraph before the last displayed equation should read "Rearranging this, we find  $c c bQ_{-i} = 2bq_i$ .
- Page 382, Duopoly section, paragraph after the displayed equation should read "...and equilibrium price becomes  $p^* = \frac{a+2c}{2+1} = \frac{a+2c}{3}$ , which also..."
- Page 386. Exercise 13, fourth line should read "...during each of thre three periods before the..."

## 13. Chapter 15.

- Page 395, previous to last paragraph should read "...are parallel to each other, but  $q_2^L(q_1)$  originates at..."
- Page 397, last paragraph should read "...yields an expected profit equal to..."
- Page 399, point 3(c), first line should read "If the highest competing bid  $h_i$  lies above  $b_i$  (see case 3c in figure 15.2), bidder *i* loses, earning a zero payoff."

## 14. Chapter 16.

- Page 423, fourth line should read "...high effort become..."
- Page 424, previous to last paragraph should read "...the positive effects offset..."
- Page 430.
  - Second line should read "if  $\frac{3}{4} p \ge 0$ , or  $p \le \frac{3}{4}$ . In this scenario, the seller's..."
  - The second expression in the second displayed equation, PC, should read "subject to  $p \leq \frac{3}{4}$ ."
- Page 432, fourth line should read " $w = \theta e^2$ . Inserting this result..."
- Page 436, last paragraph should read "...with low cost of effort because  $e_L^{SI} = e_L^{AI} = \frac{1}{\sqrt{2}}$ . This is often..."
- Page 439. Line 5 should read "...to the uninformed firm. As discussed..."
- Page 440. Delete the number 1 in the paragraph after the last displayed equation.

#### 15. Chapter 17.

• Page 448. Example 17.2. Line 14 should read "Differenting with respect to q yields  $(10 - 2q - 2) - 6\alpha^2 q = 0$ , which simplifies to  $8 = 2(q + 6\alpha^2)$ . Solving for output q, we obtain that the social optimum is

$$q^{SO} = \frac{8}{2+6\alpha^2},$$

- Page 449.
  - The label at the bottom of figure 17.2 should read  $q^{SO} = \frac{8}{2+6\alpha^2}$ .
  - First line should read "whereas  $\frac{\partial EC}{\partial q} = 6\alpha^2 q$  is a straight line starting from the origin and growing at a rate of  $6\alpha^2$ ."
  - Line 4 should read "...crosses marginal damage, at  $q^{SO} = \frac{8}{2+6\alpha^2}$ ."
  - Line 9 should read "...the socially optimal output  $q^{SO} = \frac{8}{2+6\alpha^2}$  decreases in..."
  - Line 12 should read "...the socially optimal output becomes  $\frac{8}{2+6(100)^2} = \frac{8}{2+6(100)^2} \simeq 0.0001$  units."
- Page 450. Example 17.3.
  - Line 3 should read "...the external cost in example 17.2. In addition, assume that  $\alpha$  satisfies  $0 \leq \alpha \leq 2$ . The social planner's problem is..."
  - Line 5 should read "Differentiating with respect to q yields  $(10 2q 2) (6\alpha^2 q + 7\alpha) = 0$ , which simplifies to  $8 - 7\alpha = q(2 + 6\alpha^2)$ . Solving for output q, we obtain that the social optimum is

$$q^{SO} = \frac{8 - 7\alpha}{2 + 6\alpha^2}$$

- Last displayed equation should read

$$\frac{\partial q^{SO}}{\partial \alpha} = \frac{-7 \left(2 + 6\alpha^2\right) - 12\alpha(8 - 7\alpha)}{\left(2 + 6\alpha^2\right)^2} \\ = \frac{-7 + 3\alpha \left(7\alpha - 16\right)}{\left(2 + 6\alpha^2\right)^2},$$

which is negative for all  $\alpha < 2.42$ , which holds given that  $\alpha$  satisfies  $0 \leq \alpha \leq 2$  by assumption.<sup>1</sup>"

- Line 12 should read "... if  $\alpha$  is large enough. In particular,  $\frac{8-7\alpha}{2+6\alpha^2} \leq 0$ , so long as..."
- Page 448. Renumber all examples, starting at Example 17.3, which should read Example 17.2.
- Page 453, section 17.3.2, fourth line should read "...or emission fees, which increase the cost..."
- Page 464, exercise 17.6, second line should read "...for  $\alpha \in [0, \frac{1}{3}]$ . Which subsidy per unit..."

<sup>&</sup>lt;sup>1</sup>To see this point, note that the denominator of the above expression,  $(2+6\alpha^2)^2$ , is unambiguously positive, and the numerator is negative if and only if  $3\alpha (7\alpha - 16) - 7 < 0$  or, alternatively,  $21\alpha^2 - 16\alpha - 7 < 0$ . Solving for  $\alpha$ , we obtain two roots:  $\alpha < 2.42$  and  $\alpha > -0.13$ . Since parameter  $\alpha$  satisfies  $\alpha \ge 0$  by assumption, the only relevant root is  $\alpha < 2.42$ .