**Example 7-2** Yeast is grown with glucose and ammonia to generate a recombinant protein ( $CH_{1.5}O_{0.4}N_{0.3}$ ). The respiratory quotient is 0.2. Determine the reaction stoichiometry if the yield coefficient for biomass from glucose is 0.3 g/g.

**Solution** From equation 7.40, we have

$$C_6H_{12}O_6 + \alpha O_2 + \beta NH_3 \rightarrow \delta CH_{1.8}O_{0.5}N_{0.2} + \epsilon CH_{1.5}O_{0.4}N_{0.3} + \zeta H_2O + \eta CO_2$$
 (7.48)

We can then write the elemental balances:

$$C: 6 = \delta + \varepsilon + \eta \tag{7.49}$$

$$H: 12 + 3\beta = 1.8\delta + 1.5\varepsilon + 2\zeta \tag{7.50}$$

O: 
$$6 + 2\alpha = 0.5\delta + 0.4\varepsilon + \zeta + 2\eta$$
 (7.51)

$$N: \beta = 0.2\delta + 0.3\varepsilon \tag{7.52}$$

with additional constraints for the respiratory quotient

$$\frac{\eta}{\alpha} = 0.2 \tag{7.53}$$

and the yield coefficient

$$\frac{\delta(24.6 \text{ g/mol})}{1(180 \text{ g/mol})} = 0.3 \tag{7.54}$$

This series of equations can be written in matrix form:

$$\begin{bmatrix} 0 & 0 & 1 & 1 & 0 & 1 \\ 0 & -3 & 1.8 & 1.5 & 2 & 0 \\ -2 & 0 & 0.5 & 0.4 & 1 & 2 \\ 0 & -1 & 0.2 & 0.3 & 0 & 0 \\ 0.2 & 0 & 0 & 0 & 0 & -1 \\ 0 & 0 & 24.6 & 0 & 0 & 0 \end{bmatrix} \times \begin{bmatrix} \alpha \\ \beta \\ \delta \\ \varepsilon \\ \zeta \\ \eta \end{bmatrix} = \begin{bmatrix} 6 \\ 12 \\ 6 \\ 0 \\ 0 \\ 54 \end{bmatrix}$$
 (7.55)

The solution to this system of equations reveals the following stoichiometry:

$$C_6H_{12}O_6 + 0.10 O_2 + 1.6 NH_3 \rightarrow 2.2 CH_{1.8}O_{0.5}N_{0.2} + 3.8 CH_{1.5}O_{0.4}N_{0.3} + 3.5 H_2O + 0.02 CO_2$$
 (7.56)