Seeing

The Computational Approach to Biological Vision

Second Edition

John P. Frisby and James V. Stone

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